



GCSE (9-1) Mathematics

J560/06 Paper 6 (Higher Tier)

Wednesday 8 November 2017 – Morning

Time allowed: 1 hour 30 minutes

You may use:

- · A scientific or graphical calculator
- · Geometrical instruments
- · Tracing paper





First name	
Last name	
Centre number	Candidate number

INSTRUCTIONS

- Use black ink. You may use an HB pencil for graphs and diagrams.
- Complete the boxes above with your name, centre number and candidate number.
- · Answer all the questions.
- Read each question carefully before you start to write your answer.
- Where appropriate, your answers should be supported with working. Marks may be given for a correct method even if the answer is incorrect.
- Write your answer to each question in the space provided.
- If additional space is required, you should use the lined page(s) at the end of this booklet. The question number(s) must be clearly shown.
- Do **not** write in the barcodes.

INFORMATION

- The total mark for this paper is **100**.
- The marks for each question are shown in brackets [].
- Use the π button on your calculator or take π to be 3.142 unless the question says otherwise.
- This document consists of 20 pages.



2

Answer all the questions.

- 1 Use the formula $s = ut + \frac{1}{2}at^2$.
 - (a) Calculate s when u = 5, t = 10 and a = 3.

$$s = (5)(10) + \frac{1}{2}(3)(10)^{2}$$

 $s = 50 + 150$
 $s = 200$

(b) Make a the subject of the formula.

$$S = vt + \frac{1}{2}at^{2}$$

$$(-vt) s - vt = \frac{1}{2}at^{2}$$

$$(\times 2) 2(s - vt) = at^{2}$$

$$(\div t^{2}) 2(s - vt) = a$$

$$(b) a = \frac{2(s - vt)}{t^{2}}$$

2 Carla runs every 3 days. She swims every Thursday.

On Thursday 9 November, Carla both runs and swims.

What will be the next date on which she both runs and swims?

Swims every Thursday Every 7 days

LCM of 3 and 7:

$$3 \times 7 = 2|$$

21 days later:

 $9 + 21 = 30$
 $\Rightarrow 30^{th}$ November [3]

 $\Rightarrow 30^{th}$ November (Thursday)

3 A shop records the time taken by its customers to complete a purchase on its website. The results from one day are summarised in this table.

Time taken (t minutes)	Number of customers	Midpoint	Midpointx frequency
0 < <i>t</i> ≤ 3	6	1.5	9
3 < <i>t</i> ≤ 6	10	4.5	45
6 < <i>t</i> ≤ 9	6	7 .5	45
9 < <i>t</i> ≤ 12	2	10.5	2۱
12 < <i>t</i> ≤ 15	1	13.5	13.5

(a) Calculate an estimate of the mean time taken.

$$Mean = \frac{9+45+45+21+13.5}{6+10+6+2+1} = \frac{133.5}{25}$$

$$= 5.34$$

	5 34	
(a)	ا د ٠٠	. minutes [4]

(b) Explain why it is not possible to use the information from this table to calculate the **exact** value of the mean time taken.

Because the exact time of each customer is not recorded:

4 Jeat is growing carrots from seed in his garden. He plants 28 carrot seeds but only 12 grow.

Jeat says

The probability of one of my carrot seeds growing is $\frac{3}{7}$

[1]

(a) Use Jeat's result to show that he is correct.

f (corrot seeds grow):

(b) A farmer uses this probability to calculate how many carrot seeds he should plant to grow 10000 carrots.

How many seeds should he plant?

10000 to grow. 10000 = 3 of what he grows $\frac{10000}{3} = \frac{1}{7} \text{ of what he grows}$ $23333 = \frac{7}{7} \text{ (all) of what he grows}$

(c) Explain why it may not be sensible for the farmer to use Jeat's experimental probability to calculate the number of seeds he should plant.

Jeat uses too small comparable to the large sample 5 A company makes sweets. The sweets are put into packets.

Here are some facts.

1.47 × 10⁷ sweets are made every day 3.5 × 10⁵
packets of sweets are produced every day

(a) Calculate the mean number of sweets in one packet.

Mean sweets in | packet = $\frac{\text{Total sweets produce}}{\text{Total packets produce}}$ mean sweets in | packet = $\frac{1.47 \times 10^7}{3.5 \times 10^5} = 42$

(a)

(b) Sweets are made on 288 days each year.

Calculate the number of sweets made each year. Give your answer in standard form.

Sweets per year = days x sweets per day = 288 x 1.47 × 107 = 4-233600000 (b) 4.2336 × 10₁₃

- (c) The company has 152 machines making the sweets. Each machine operates for 15 hours each day.
 - (i) Calculate the number of sweets made by one machine each hour. Give your answer as an ordinary number correct to the nearest 10.

Per machine: $(1.47 \times 10^7) \div 152 = 96710.5 \approx 96711$ Per machine per hour: $96711 \div 15 = 6447.4$ To rearest 10:6450 6450

(ii) State one assumption you have made in part (c)(i).

fill machines make sweets at the same rate for the whole time. [1]

6 (a) Two bags each contain only red counters and yellow counters.

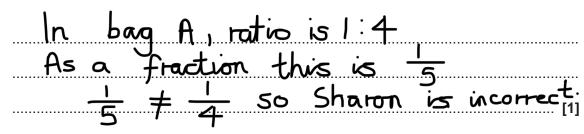
In Bag A, the ratio of red counters to yellow counters is 1 : 4.

In Bag B, $\frac{1}{4}$ of the counters are red.

(i) Sharon says

The proportion of the counters that are red is the same in both bags.

Explain why Sharon is not correct.



(ii) The number of counters in the two bags is the same.

Complete the table below to show how many counters of each colour could be in the bags.

Bag A: Yellow =
$$4 \times \text{red}$$

Bag B: Yellow = $3 \times \text{red}$
 $4 + R_A = 4 + R_B$
 $\frac{1}{4} = \frac{5}{20}$
 $\frac{1}{5} = \frac{4}{20}$

YA = yellor	J in A
Ra= red	
YB = yello	winB
RB = red	in B

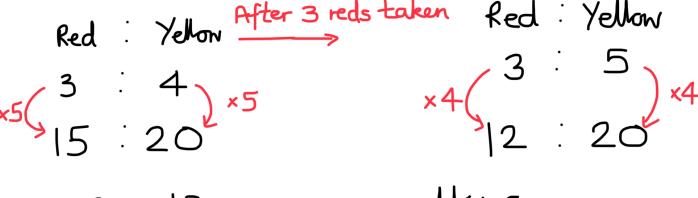
	Red counters	Yellow counters
Bag A	4	16
Bag B	5	15

[3]

7

(b) In another bag, Bag C, the ratio of red counters to yellow counters is 3 : 4. If 3 of the red counters are removed from Bag C, the ratio of red counters to yellow counters is 3 : 5.

How many **yellow** counters are in Bag C?



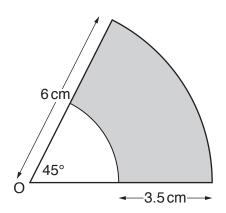
7 Gustavo invests £520 for 6 years in a bank account paying simple interest. At the end of 6 years, the amount in the bank account is £629.20.

Calculate the annual rate of interest.

Total interest:
$$629.20 - 520 = £109.20$$

Interest per year: $109.20 \div 6 = £18.20$
Proportion of initial investment: $\frac{18.20}{520} \times 100$
 $\frac{18.20}{520} \times 100$

8 The design below is made from two sectors of circles, centre O.



Calculate the perimeter of the shaded part. Give your answer correct to 3 significant figures.

Gramference of whole circle =
$$2\pi r$$

$$= 2 \times \pi \times 6 = 12\pi$$
Proportion of circle: $\frac{45}{360}$ (360° in whole circle)
$$\frac{45}{360} \times 12\pi = \frac{1}{8} \times 12\pi = 1.5\pi \text{ cm}$$
Radius = $6-3.5=2.5\text{ cm}$
Circumference = $2 \times 2.5 \times \pi$

$$= 5\pi$$

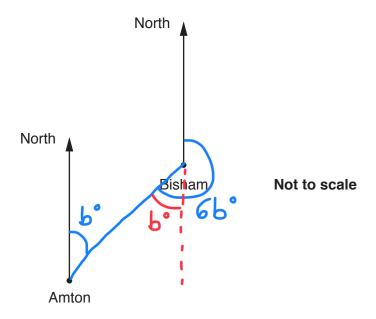
$$\frac{45}{360} \times 5\pi = \frac{1}{8} \times 5\pi = 0.625\pi \text{ cm}$$

$$3.5 + 3.5 = 7\text{ cm}$$
Whole perimeter: $1.5\pi + 0.625\pi + 7$

$$= 13.7 \times 3.5 = 12\pi$$
Whole perimeter: $1.5\pi + 0.625\pi + 7$

$$= 13.7 \times 3.5 = 12\pi$$

9 The diagram shows the positions of two towns, Amton and Bisham.



The bearing of Bisham from Amton is b° . The bearing of Amton from Bisham is $6b^{\circ}$.

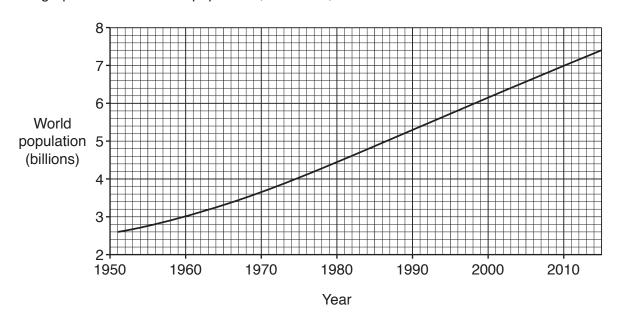
Calculate the 3-figure bearing of Amton from Bisham.

$$6b = 180 + b$$

 $5b = 180$
 $b = 36$
 $6b = 6 \times 36 = 216^{\circ}$

2/6 [4]

This graph shows the world population, in billions, between 1951 and 2015.



Use the graph to estimate the average rate of growth of the world population between 1951 and 2015.

Give suitable units for your answer.

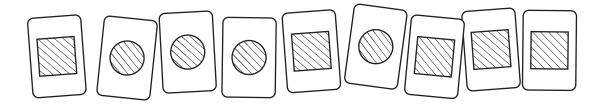
Rate of growth = gradient of graph:

$$(x_1, y_1) = (1960, 3)$$

 $(x_2, y_2) = (2010, 7)$
 $(x_2, y_2) = (2010, 7)$

gradient = $\frac{y_2 - y_1}{x_2 - x_1} = \frac{7 - 3}{2010 - 1960} = \frac{4}{50} = 0.08$

11 Reuben is playing a matching game with these cards.

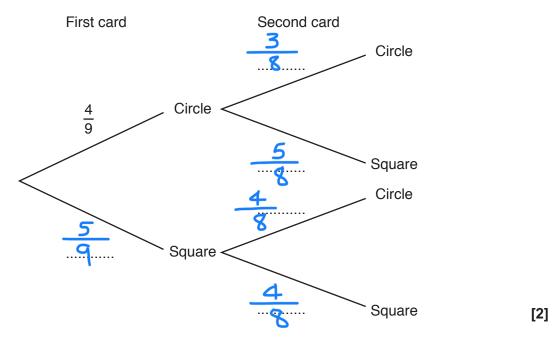


He turns the cards over and shuffles them.

Reuben takes a card and keeps it. He then takes a second card.

If the cards are different, he wins the game.

(a) Complete this tree diagram to show the probabilities for each card picked in the game.



P(circle, Square):
$$\frac{4}{9} \times \frac{5}{8} = \frac{20}{72}$$

P(square, circle): $\frac{5}{9} \times \frac{4}{8} = \frac{20}{72}$

P(circle and square in either $\frac{5}{9}$

order): $\frac{20}{72} + \frac{20}{72} = \frac{40}{72}$

12 (a) A sequence is defined using this term-to-term rule.

$$u_{n+1} = \sqrt{2u_n + 15}$$

If $u_1 = 5$, find u_2 .

$$U_{2} = \sqrt{2(5) + 15}$$

$$= \sqrt{25} = 5$$
(a) (a) [1]

(b) Another sequence is defined using this term-to-term rule,

$$u_{n+1} = ku_n + r$$

where *k* and *r* are constants.

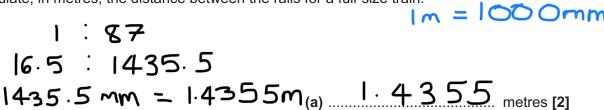
Given that u_2 = 41, u_3 = 206 and u_4 = 1031, find the value of k and the value of r.

$$\begin{array}{l} U_{n+1} = k U_{n} + r \\ U_{3} = 4lk + r = 206 & 0 \\ U_{4} = 206k + r = 1031 & 0 \\ \hline 2 - 0 : 206k + r = 1031 \\ \hline -4k + r = 206 \\ \hline 165k + (b)^{0}k = 825 & 5 \\ \hline k = 5 & r = 1 \end{array}$$

- **13** A model railway is built using the scale 1 : 87.
 - (a) On the model railway, the distance between the rails is 16.5 mm.



Calculate, in metres, the distance between the rails for a full-size train.



(b) The volume of a full-size train carriage is 220 m³.

16.5:1435.5

1: ダア

Trevor calculates the volume of a model train carriage to be 334 cm³ correct to 3 significant figures.

Is Trevor's calculation correct? Show how you decide.

$$220m^3 \rightarrow cm^3$$

 $220m^3 = 220 \times |00^3 = 22000000$

Volume of model train: 220000000 ÷ 873 = 334.09cm = 334cm (to rearest cm)

levor's calculation is [3]

14 The diagram shows a cross placed on a number grid.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60

L is the product of the left and right numbers of the cross.

T is the product of the top and bottom numbers of the cross.

M is the middle number of the cross.

(a) Show that when
$$M = 35$$
, $L - T = 99$.

$$L = 34 \times 36 = 1224$$

 $T = 45 \times 25 = 1125$
 $L - T = 1224 - 1125 = 99$

(b) Prove that, for any position of the cross on the number grid above, L - T = 99.

[2]

[5]

 $OCR 2017 = M^2 - M^2 + |OO - | = |OO - | =$

15 The following formula is for the area, A, of the curved surface area of a cone. $A = \pi r I$, where r is the radius and I is the slant height of the cone.

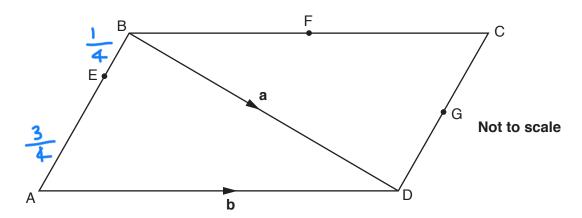
Calculate the **total** surface area of a cone with radius 5 cm and slant height 12 cm.

Curred surface area:
$$A = \pi \times 8 \times 12 = 60\pi$$

Flat surface area: $A = \pi r^2 = \pi \times 5^2$
= 25 π

Total surface area: $60\pi + 25\pi = 85\pi \text{cm}^2$

16 ABCD is a parallelogram.



 $\overrightarrow{BD} = \mathbf{a}$ and $\overrightarrow{AD} = \mathbf{b}$. F is the midpoint of BC. G is the midpoint of DC. AE = 3EB.

(a) Write down simplified expressions in terms of a and b for

(i)
$$\overrightarrow{AB}$$
, = \overrightarrow{AD} + \overrightarrow{DB}
= \underline{b} - \underline{a}
(a)(i) \underline{b} - \underline{a}

(ii)
$$\overrightarrow{BB} = \frac{3}{4} (\overrightarrow{AB})$$

$$= \frac{1}{4} \underline{b} - \frac{1}{4} \underline{q}$$

(ii)
$$\frac{1}{4} \underline{b} - \frac{1}{4} \underline{a}$$
 [1]

[2]

(b) Show that
$$\overrightarrow{EF} = \frac{1}{4}(3\mathbf{b} - \mathbf{a})$$
.

$$\overrightarrow{BF} : \overrightarrow{BG} = \overrightarrow{AD} \quad \overrightarrow{BF} = \frac{1}{2} \overrightarrow{BG} = \frac{1}{2} \underline{b}$$

$$\overrightarrow{BF} : \overrightarrow{BG} = \frac{1}{4} \underline{b} - \frac{1}{4} \underline{q} + \frac{1}{2} \underline{b} = \frac{3}{4} \underline{b} - \frac{1}{4} \underline{q}$$

(c) Prove that
$$\overrightarrow{\mathsf{EF}}$$
 and $\overrightarrow{\mathsf{AG}}$ are parallel.

$$= \frac{1}{4} \left(3 \underline{b} - \underline{\alpha} \right)$$

$$\overrightarrow{AG} = \overrightarrow{AD} + \overrightarrow{DG} \rightarrow \overrightarrow{DG} = \frac{1}{2} \underline{b} - \frac{1}{2} \underline{q}$$

$$\overrightarrow{DG} : \overrightarrow{AB} = \overrightarrow{DC} \rightarrow \overrightarrow{AG} = \underline{b} + \frac{1}{2} \underline{b} - \frac{1}{2} \underline{q}$$

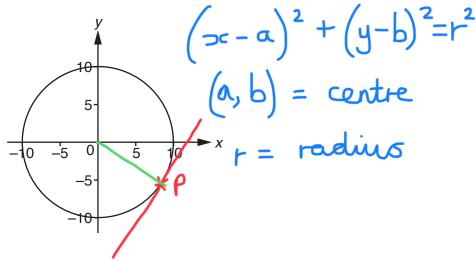
$$\overrightarrow{DC} = \underline{b} - \underline{q} \rightarrow \underline{q}$$

$$= \underline{3} \underline{b} - \frac{1}{2} \underline{q}$$

$$= \underline{3} \underline{b} - \underline{1} \underline{q}$$

 \overrightarrow{AG} is a multiple of $\overrightarrow{EF}(x2)$ so they are parallel.

17 The diagram shows a circle, centre the origin.



(a) Write down the equation of the circle.

centre =
$$(0,0)$$
 radius = 10

(a)
$$\chi^2 + \eta^2 = 100_{[1]}$$

[2]

(b) Point P has coordinates (8, −6). Show that point P lies on the circle.

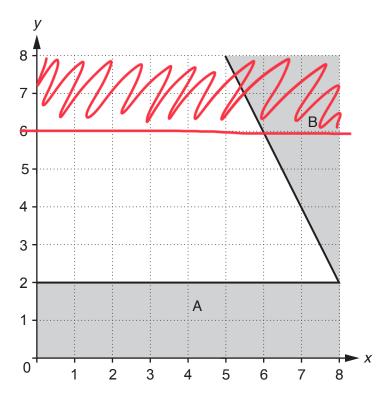
sub in x = 8, y = -6: $(8)^2 + (-6)^2$ = 100 so it is on the circle.

(c) Find the equation of the tangent to the circle at point P.

gradient of normal:
$$(-6-0) = -\frac{3}{4}$$

gradient of tangent: $-\frac{3}{4} \rightarrow \frac{4}{3}$
 $y = \frac{4}{3}x + C$
 $-6 = \frac{4}{3}(8) + C$
 $c = -50$
 $3y = 4x - 50$
 $3y - 4x + 50 = 0$

The diagram below shows a 1cm coordinate grid.



(a) Find an inequality that defines region A and another inequality that defines region B.

$$A: y \leq 2$$

B: gradient of line =
$$\frac{y_2 - y_1}{x_2 - x_1} = \frac{8 - 2}{5 - 8}$$

$$y = -2x + c$$

$$5ub (5,8) : 8 = -2(5) + c$$

$$c = 18$$

$$y = -2x + 18$$
(a) Region A: $y \le 2$
Region B: $y \ge -2x$

Region B: $y \ge -2x + 18$ _[4]

(b) Shade the region on the grid given by the inequality $y \ge 6$.

[2]

→ Draw line 4= 6

→ y ≥ 6 (y is greater or equal to 6) so shade above

(c) A fourth shaded region, given by the inequality

e inequality
$$y \ge kx + 2,$$

$$\frac{1}{2}(a+b) \times h$$

is added to the grid.

The unshaded region now has area 23 cm².

Find the value of k.

$$y \ge kx + 2$$

huight = 6-2=4
 $b = 8$
 $\frac{1}{2}(a+8) \times 4 = 23$
 $2a + 16 = 23$

$$a = 3.5$$

Therefore, top of trapezium = 3.5 squares

$$\rightarrow x$$
 - coordinate = $6-3.5=2.5$
qradient (k)

(c) $k = \frac{8}{5}$

[5]

$$= \frac{y_2 - y_1}{3c_2 - x_1} = \frac{6 - 2}{2 \cdot 5 - 6} = \frac{\text{END OF QUESTION PAPER}}{2 \cdot 5}$$

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ADDITIONAL ANSWER SPACE

If additiona must be cle	I space is required, you should use the following lined page(s). arly shown in the margin(s).	The question number(s)
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